

# Thermodynamic, structural and surface properties of rare earth metallic alloys: Au-La liquid system

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## Abstract

A complete information related to the mixing behaviours of Au alloyed with rare earth metals or lanthanides is very scarce. Therefore, an attempt has been made in this work to compute and study the temperature and concentration dependent thermodynamic, structural and surface properties of Au-La liquid alloy using different theoretical approaches. The thermodynamic properties, such as excess Gibbs free energy of mixing, enthalpy of mixing, excess entropy of mixing and activity of the system were computed using available coefficients of interaction energy parameters in the framework of Redlich-Kister polynomial. Taking these as reference values, model parameters for quasi-lattice model were optimised at 1473 K. The model parameters were then determined at higher temperatures assuming them to be linear temperature-dependent. The thermodynamic and structural properties were then computed in the temperature range 1473 K-1773 K. The surface properties of the system were computed using Bulter's model using determined values of partial excess Gibbs free energy of its components. Present investigations revealed that the compound forming tendency of the system gradually decreased with increase in temperature of the system.

## Keywords

Ordering energy, hetero-coordinating nature, segregating nature, surface segregation, surface tension.

## Article information

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## 1 Introduction

Development of lead free solders has been a great task for the researchers working in the field of materials design and fabrication. One of the most promising alternative for the purpose has been found to be the use of Sn-based alloys, more precisely Sn-Ag-Cu ternary alloys. Addition of small amount of rare earth (RE) elements to these alloys, increases the mechanical behaviour, creep-fatigue resistance and wetting properties [1–4]. In due course, knowledge related to the mixing behaviours

of RE-based liquid alloys are important. But a very few information regarding the thermo-physical properties of metallic alloys having RE metals, also called lanthanide, as ingredient is available to date. In order to develop the thermodynamic database of RE-based liquid alloy, the thermodynamic and structural properties of Au-La liquid alloy was studied in the previous work [5]. To further enhance the procedure, the mixing properties of Au-La liquid alloy have been computed and studied at different

temperatures in the present work.

Dong et al. in 2011 [6] have summarized the details of literature associated with the works carried out by different researchers to assess the mixing properties of Au-La alloy. In their work, phase relations in Au-La and Au-Er alloys have been thermodynamically studies using CALPHAD technique incorporated with the ab initio calculations. They calculated enthalpy of mixing of the system at 1473 K and compared them with the experimental values of Fitzner et al. [7]. Further, they presented the self consistent parameters of Redlich-Kister polynomial [8] for the excess Gibbs free energy of mixing for different phases present in the alloy. They calculated the existence of different stable phases, such as  $AuLa_2$ ,  $AuLa$ ,  $Au_2La$ ,  $Au_{51}La_{14}$  and  $Au_6La$ . These results were found to be in good agreement with those obtained by Massalski [9], except for the reaction temperature and composition involving the constitution of  $Au_2La$  and  $Au_{51}La_{14}$  phases. They found the reaction temperature to be 75 K higher and close to  $x_{Au} = 0.04$  than observed by Massalski. In the knowledge of the author of this work, the complete description of the mixing properties of the system is lacking to date.

Therefore, an attempt has been made in this work to study and explain the thermodynamic, structural and surface properties of the liquid alloy at different temperatures. In thermodynamic properties, such as excess Gibbs free energy of mixing ( $\Delta G_M^{xs}$ ), enthalpy of mixing ( $\Delta H_M$ ), entropy of mixing ( $\Delta S_M^{xs}$ ) and activity ( $a_i$ ;  $i = Au, La$ ) were computed using modeling equations of quasi-lattice model. In the same frame, the structural properties, such as concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ), Warren-Cowley short range order parameter ( $\alpha_1$ ) and ratio of mutual to intrinsic diffusion coefficients ( $D_M/D_{id}$ ) were calculated. The surface tension and surface concentrations of the system were calculated using Butler's model [10–13].

## 2 Formulations

### 2.1 Quasi-lattice model

This theoretical approach assumes that when two elements A and B are mixed in liquid state, the formation of the complex of the type  $A_\mu B_\nu$  takes place. The values of  $\mu$  and  $\nu$  depend upon stoichiometric compositions at which the stable phase is present and are determined from the phase diagram of the system. In this work, the existence of the complex  $Au_2La$  [6, 7] was considered as energetically favoured. In this regard, the expression for excess Gibbs free energy of mixing ( $\Delta G_M^{xs}$ ) can be given as [14–16]

$$\Delta G_M^{xs} = N[\Phi\omega + \Phi_{AB}\omega_{AB} + \Phi_{AA}\omega_{AA}] \quad (1)$$

where  $\omega$ ,  $\omega_{AB}$  and  $\omega_{AA}$  are the interaction energy or model parameters. They are assumed to be temperature-dependent but concentration independent.  $\Phi$ ,  $\Phi_{AB}$  and  $\Phi_{AA}$  are the simple polynomials in  $x_1$  and  $x_2$ , such that  $x_1 + x_2 = 1$ .  $\Phi$ ,  $\Phi_{AB}$  and  $\Phi_{AA}$  are expressed as [14–16]

$$\begin{aligned} \Phi &= x_1x_2 \\ \Phi_{AB} &= \frac{x_1}{6} + x_1^2 - \frac{5x_1^3}{3} + \frac{x_1^4}{2} \\ \Phi_{AA} &= -\frac{x_1}{4} + \frac{x_1^2}{2} - \frac{x_1^4}{4} \end{aligned} \quad (2)$$

$\Delta G_M^{xs}$  can be expressed in terms of Gibbs free energy of mixing ( $\Delta G_M$ ) as

$$\Delta G_M = \Delta G_M^{xs} + RT[x_1 \ln x_1 + x_2 \ln x_2] \quad (3)$$

where R (in J/(mol.K)) is the real gas constant and T (in K) is the absolute temperature. The excess entropy of mixing ( $S_M^{xs}$ ) is related to  $\Delta G_M^{xs}$  as

$$\Delta S_M^{xs} = - \left( \frac{\partial \Delta G_M^{xs}}{\partial T} \right)_P \quad (4)$$

From Equations (1) and (4), one can obtain

$$\Delta S_M^{xs} = -N \left[ \frac{\partial \Delta \omega}{\partial T} \Phi + \frac{\partial \Delta \omega_{AB}}{\partial T} \Phi_{AB} + \frac{\partial \Delta \omega_{AA}}{\partial T} \Phi_{AA} \right] \quad (5)$$

Herein,  $\frac{\partial \Delta \omega}{\partial T}$ ,  $\frac{\partial \Delta \omega_{AB}}{\partial T}$  and  $\frac{\partial \Delta \omega_{AA}}{\partial T}$  are the temperature derivative terms of interaction energy parameters.

The enthalpy of mixing ( $\Delta H_M$ ) can be related to  $\Delta G_M^{xs}$  and  $\Delta S_M^{xs}$  by the well known thermodynamic expression as

$$\Delta H_M = \Delta G_M^{xs} + T\Delta S_M^{xs} \quad (6)$$

Using Equation (4) in Equation (6), yields

$$\Delta H_M = \Delta G_M^{xs} - T \left( \frac{\partial \Delta G_M^{xs}}{\partial T} \right)_P \quad (7)$$

The activity of component  $i$  ( $a_i$ ;  $i = Au, La$ ) in the binary solution can be expressed in terms of  $\Delta G_M$  as

$$RT \ln a_i = \Delta G_M + (1 - x_i) \left( \frac{\partial \Delta G_M}{\partial x_i} \right)_{T,P,N} \quad (8)$$

Using Equations (1) and (3) in Equation (8), one can obtain the expression for  $\left( \frac{\partial \Delta G_M}{\partial x_i} \right)_{T,P,N}$  as

$$\left(\frac{\partial \Delta G_M}{\partial x_i}\right)_{T,P,N} = \Delta \omega \Phi' + \Delta \omega_{AB} \Phi_{AB}' + \Delta \omega_{AA} \Phi_{AA}' + \ln\left(\frac{x_i}{1-x_i}\right) \quad (9)$$

where  $\Phi'$  and  $\Phi'_{ij}$  are the first order derivatives of respective parameters (in Equation (2)) with respect to concentration of  $i^{\text{th}}$  element.

To study and understand the arrangement of atoms at atomic level in the initial melt, the structural functions have become an essential tool. Among them, the expression for concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ) is expressed as [17–20]

$$S_{CC}(0) = RT \left(\frac{\partial^2 G_M}{\partial x_1^2}\right)_{T,P,N}^{-1} = RT \left(\frac{\partial^2 G_M}{\partial x_2^2}\right)_{T,P,N}^{-1} \quad (10)$$

Using Equations (1) and (3) in Equation (10), yields

$$S_{CC}(0) = x_1 x_2 [1 + x_1 x_2 RT (\Delta \omega \Phi'' + \Delta \omega_{AB} \Phi_{AB}'' + \Delta \omega_{AA} \Phi_{AA}'')]^{-1} \quad (11)$$

where  $\phi''$  and  $\phi''_{ij}$  are the second order derivatives of respective parameters with respect to concentration ( $x_i$ ) and can be obtained from Equation (2). The ideal values of  $S_{CC}(0)$  is obtained by the following relation

$$S_{CC}^{id}(0) = x_1 x_2 \quad (12)$$

The structural functions, Warren-Cowley short range-order parameter ( $\alpha_1$ ) and the ratio of mutual to intrinsic diffusion coefficients ( $D_M/D_{id}$ ) can be expressed in terms of  $S_{CC}(0)$  as [13, 15, 18, 21]

$$\alpha_1 = \frac{S - 1}{[S(Z - 1) + 1]} \quad (13)$$

with

$$S = \frac{S_{CC}(0)}{S_{CC}^{id}(0)} \quad (14)$$

and

$$\frac{D_M}{D_{id}} = \frac{S_{CC}^{id}(0)}{S_{CC}(0)} \quad (15)$$

## 2.2 Redlich-Kister (R-K) polynomial

R-K polynomial is used to model the temperature-dependent thermodynamic properties of liquid alloys. It is extensively used as modeling equations in theoretical calculations, software based computations and experimental measurements [6, 8]. In this approach,  $\Delta G_M^{xs}$  is expressed as [5, 6, 8, 22]

$$\Delta G_M^{xs} = x_1 x_2 \sum_{q=0}^n L_q (x_1 - x_2)^q \quad (16)$$

where  $L_q$  are the linear T-dependent coefficients or interaction energy parameters of R-K polynomial. They are expressed in the form  $L_q = a_q + b_q T$ , where  $a_q$  (in J/mol) are contributions due to  $\Delta H_M$  and  $b_q$  (in J/mol-K) are contributions of  $\Delta S_M^{xs}$  to  $\Delta G_M^{xs}$  equivalent to Equations 6.

The partial excess Gibbs free energy ( $\Delta G_i^{xs}$ ) of the component  $i$  in the binary liquid alloy can be given as [22]

$$\Delta G_i^{xs} = \Delta G_M^{xs} + (1 - x_i) \left(\frac{\partial \Delta G_M^{xs}}{\partial x_i} - \frac{\partial \Delta G_M^{xs}}{\partial (1 - x_i)}\right) \quad (17)$$

The activity coefficient of component  $i$  in the binary solution is related to  $\Delta G_i^{xs}$  as

$$RT \ln \gamma_i = \Delta G_i^{xs} \quad (18)$$

After the computations of  $\gamma_i$ , the activity of component  $i$  can be obtained by the relation

$$a_i = x_i \gamma_i \quad (19)$$

The values of  $S_M^{xs}$  and  $H_M$  can be obtained using Equations (4), (7) and (16). Using Equations (10) and (16),  $S_{CC}(0)$  for this system having  $q = 0, 1$  can be obtained as [5, 23]

$$S_{CC}(0) = RT[-2L_0 + (-12x_1 + 6)L_1 + \frac{RT}{x_1(1-x_1)}]^{-1} \quad (20)$$

The values of other structural functions in this framework can also be obtained using Equations (13-15).

## 2.3 Butler model

The surface properties, surface tension ( $\sigma$ ) and surface concentrations ( $x_i^s$ ) of the system have been calculated using Butler model. According to this model,  $\sigma$  for binary liquid solution can be given as [10–13]

$$\begin{aligned}\sigma &= \sigma_1 + \frac{RT}{A_1} \ln \frac{x_1^S}{x_1^b} + \frac{\Delta G_{1,S}^{xs} - \Delta G_{1,b}^{xs}}{A_1} \\ &= \sigma_2 + \frac{RT}{A_2} \ln \frac{x_2^S}{x_2^b} + \frac{\Delta G_{2,S}^{xs} - \Delta G_{2,b}^{xs}}{A_1}\end{aligned}\quad (21)$$

where  $\sigma_i$  is the surface tension,  $A_i$  is molar surface area,  $x_i^S$  is the surface concentration,  $x_i^b$  is the bulk concentration,  $\Delta G_{i,S}^{xs}$  is the molar surface partial excess Gibbs free energy and  $\Delta G_{i,b}^{xs}$  is the molar bulk partial excess Gibbs free energy for the component  $i$  of the liquid mixture at the melting temperature of the alloy.  $\Delta G_{i,S}^{xs}$  and  $\Delta G_{i,b}^{xs}$  related by the relation

$$\Delta G_{i,S}^{xs} = \beta \Delta G_{i,b}^{xs} \quad (22)$$

where  $\beta = 0.8181$  [11, 13] for simple liquid metals. The molar surface area ( $A_i$ ) of component  $i$  in the liquid mixture can be calculated using the relation

$$A_i = f N_A^{\frac{1}{3}} V_i^{\frac{2}{3}} \quad (23)$$

where  $N_A$  is the Avogadro's number and  $V_i (= \frac{m_i}{\rho_i})$  is the molar volume of element  $i$  in the liquid mixture. The values of  $\sigma_i$  and  $V_i$  are calculated with the help of the following relations [11, 24]

$$\sigma_i = \sigma_i^0 + \frac{d\sigma}{dT}(T - T_0) \quad (24)$$

and

$$V_i = V_i^0 [1 + \lambda_i (T - T_0)] \quad (25)$$

where  $\sigma_i^0$  is the surface tension,  $V_i^0$  is the molar volume and  $\lambda_i$  [11, 24] is the temperature coefficient of volume expansion for  $i^{\text{th}}$  component at its melting temperature ( $T_0$ ).

### 3 Results and Discussion

#### 3.1 Thermodynamic properties

The self-consistent parameters for excess Gibbs free energy of mixing ( $\Delta G_M^{xs}$ ) of Au–La liquid alloy were taken from Dong et al. [6] (Table 1). These parameters were used to calculate  $\Delta G_M^{xs}$  of the system at 1473 K in the frame work of R-K polynomial [8] (Equation (16)). The values so computed were considered as reference data and then quasi-lattice model was employed to determine the model fit parameters using Equations (1-3). The best fit values of the model parameters were estimated assuming the existence of  $Au_2La$  complex and are presented in Table 1.

Table 1: Interaction energy parameters for  $\Delta G_M^{xs}$  of Au–La liquid alloy

Parameters [J/mol]	Reference
$L_0 = -254446.24 + 6.00025 * T$ $L_1 = -85046.07 + 2.89377 * T$	[6]
$\Delta\omega = -264279.94476 + 8.97912 * dT$ $\Delta\omega_{AB} = -3042.03606 + 0.083140 * dT$ $\Delta\omega_{AA} = -345964.24650 + 1.66280 * dT$	This work

The determined values of model parameters  $\Delta\omega$ ,  $\Delta\omega_{AB}$  and  $\Delta\omega_{AA}$  were found to have negative values (Table 1). Among them,  $\Delta\omega$  is called ordering energy parameter and its value was estimated to be  $-264279.94476$  indicating the system to be strongly interacting in nature. The value of  $\Delta G_M^{xs}$  was computed at 1473 K using the parameters from Table 1 and Equations (1-3). The compositional dependence of  $\Delta G_M^{xs}$  of the this work along with the values computed using the parameters of Dong et al. are displayed in Figure 1.

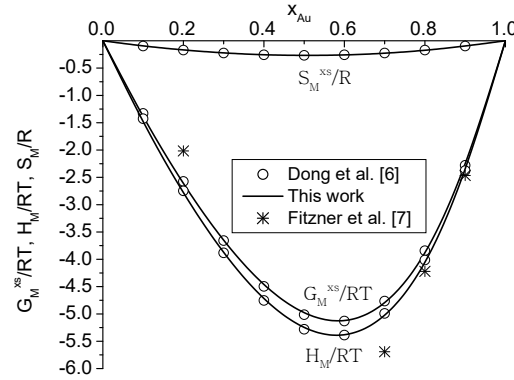


Figure 1: Compositional dependence of  $\Delta G_M^{xs}/RT$ ,  $\Delta H_M/RT$  and  $\Delta S_M^{xs}/R$  of Au–La liquid alloy at 1473 K.

The computed values of  $\Delta G_M^{xs}$  were found to be in consistent with each other at compositions thereby validating the present optimisation procedure (Figure 1). The maximum negative value of  $\Delta G_M^{xs} = -5.12014RT$  (this work) and  $\Delta G_M^{xs} = -5.12991RT$  (Dong et al.) [6] at  $x_{Au} = 0.6$ . The high negative value of  $\Delta G_M^{xs}/RT$  indicates the system to be strongly interacting in nature at its melting temperature, 1473 K. Moreover, the system is found to be asymmetric with respect to  $\Delta G_M^{xs}$ .

The enthalpy of mixing ( $\Delta H_M/RT$ ) and excess entropy of mixing  $\Delta S_M^{xs}/R$  of the system were calculated with the help of parameters from Table 1 and Equations (4-7). These computed values are portrayed as a function of composition in Figure 1.

The extremum negative value of  $\Delta H_M/RT = -5.37922RT$  (this work) and  $\Delta H_M/RT = -5.38665RT$  (Dong et al. [6]) at  $x_{Au} = 0.6$ . The high negative value of  $H_M/RT$  corresponds the strong association between Au and La in the assumed complex at 1473 K. Further, the computed values of  $\Delta H_M/RT$  of this work and those of Dong et al. were consistent with each other and the system is found to be asymmetric with respect this physical function. The values of  $\Delta H_M/RT$  were also found to be in agreement with the experimental values of Fitzner et al. [7] at higher compositions of Au. Likewise, the maximum negative value of  $\Delta S_M^{xs} = -0.26781R$  (this work) and  $\Delta S_M^{xs} = -0.26744R$  (Dong et al.) at  $x_{Au} = 0.5$ . The Au-La liquid alloy is found to be symmetric with respect to  $\Delta S_M^{xs}$ . Thus, the above theoretical investigations reveal that the model parameters determined in the frame work of quasi-lattice model are fruitful in explaining the thermodynamic properties of the system.

To further validate the present optimisation process, the activity of the system was computed using the same determined model parameters. The activities of the individual atoms ( $a_{Au}$  and  $a_{La}$ ) of the initial melt were calculated on the basis of R-K polynomial (Equations (16-19)) and quasi-lattice model (Equations (8 and 9)) using the parameters from Table 1. The calculated and ideal values of  $a_{Au}$  and  $a_{La}$  are plotted as a function of concentration in Figure 2.

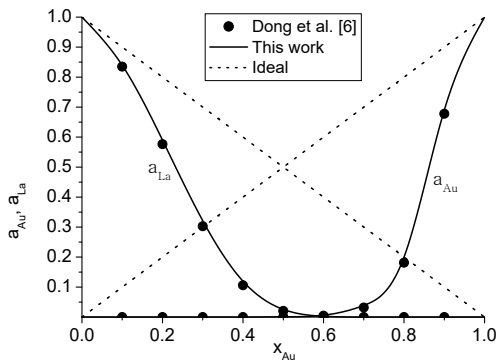


Figure 2: Computed values of  $a_{Au}$  and  $a_{La}$  versus concentration of Au ( $x_{Au}$ ) of Au-La liquid alloy at 1473 K.

The computed values of  $a_{Au}$  and  $a_{La}$  were found to be much less than their respective ideal values at all compositions indicating the system to be strongly interacting in nature. Both of these values, computed using the parameters of present work and Dong et al., were found to be consistent with each

other at all concentrations (Figure 2). Thus, it can be stated that the preferred model is capable of explaining the thermodynamic functions and reproducing the activity of the system. Therefore, these model parameters were considered for the computations of structural and surface properties.

In thermodynamic properties,  $\Delta G_M^{xs}$ ,  $\Delta H_M$  and  $a_i$ ;  $i = Au, La$  were computed at different temperatures assuming the model parameters of quasi-lattice model to be linear temperature-dependent. The model parameters  $\Delta\omega$ ,  $\Delta\omega_{AB}$  and  $\Delta\omega_{AA}$  in correlation with their respective temperature derivatives terms  $\partial\Delta\omega/\partial T$ ,  $\partial\Delta\omega_{AB}/\partial T$  and  $\partial\Delta\omega_{AA}/\partial T$  can be expressed as [5, 13]

$$\Delta\omega(T) = \Delta\omega(T_0) + \frac{\partial\Delta\omega}{\partial T}(T - T_0) \quad (26)$$

$$\Delta\omega_{ij}(T) = \Delta\omega_{ij}(T_0) + \frac{\partial\Delta\omega_{ij}}{\partial T}(T - T_0) \quad (27)$$

where  $T_0$  ( $= 1473$  K) is the melting temperature of the system and  $T$  is the temperature of interest at which thermodynamic properties are to be calculated. The determined values of temperature-dependent model parameters for this liquid alloy are portrayed in Table 1.

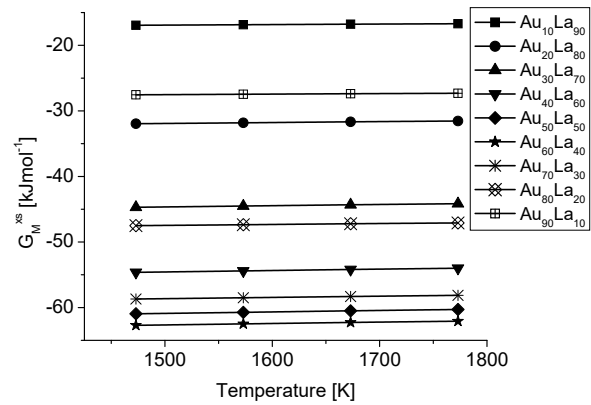


Figure 3: Temperature dependence of excess Gibbs free energy of mixing ( $\Delta G_M^{xs}$ ) for Au-La liquid alloy.

The values of  $\Delta G_M^{xs}$  were computed using Equations (1 and 2),  $\Delta H_M$  were computed using Equations (1 and 7) and  $a_i$  were computed using Equations (17-19) at different temperatures with the aid of parameters in Table 1. The temperature variation of  $\Delta G_M^{xs}$  and  $\Delta H_M$  at fixed composition ratios of Au and La are presented in Figures 3 and 4. The compositional dependence of  $a_i$  at different temperatures are plotted in Figures 5 and 6.

The negative values of  $\Delta G_M^{xs}$  and  $\Delta H_M$  decreased linearly with increased in temperature of the system.

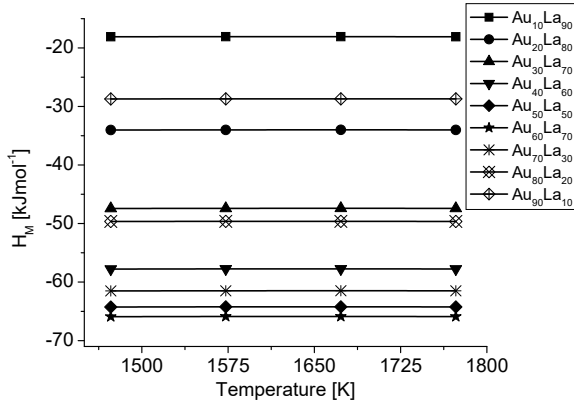


Figure 4: Variation of  $\Delta H_M$  with temperature of Au-La liquid alloy.

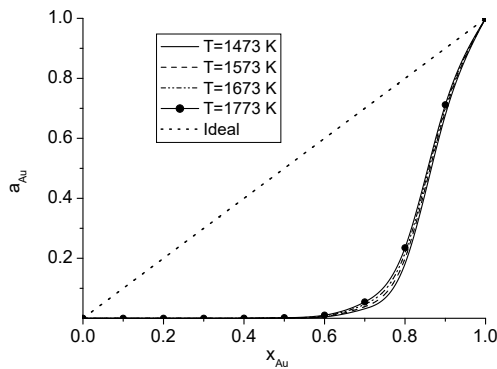


Figure 5: Activity of Au ( $a_{Au}$ ) versus  $x_{Au}$  in temperature range 1474–1773 K.

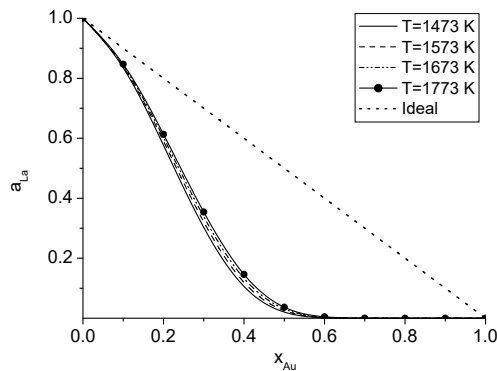


Figure 6: Compositional dependence of activity of La ( $a_{La}$ ) at different temperatures.

These results revealed the decrease in the complex

formation tendency or strength of interaction between the monomers. Indeed, the activities of Au and La gradually increased with increase in temperature. The deviation of  $a_i$  from ideal values gradually decreased with increase in temperature indicating the decrease in mixing tendency of the system (Figures 5 and 6).

### 3.2 Structural properties

The information related to the local arrangement of atoms in the initial melt can be obtained from the knowledge of structural functions. In structural functions, concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ), Warren-Cowley short range order parameter ( $\alpha_1$ ) and ratio of mutual to intrinsic diffusion coefficients ( $D_M/D_{id}$ ) were computed in the frame work of quasi-lattice model using Equations (10-15) and parameters from Table 1. Likewise, Equations (12-15) and (20) were used to calculate these values on the basis of R-K polynomial with the aid of parameters of Dong et al. (Table 1). The compositional dependence of  $S_{CC}(0)$ ,  $\alpha_1$  and  $D_M/D_{id}$  are plotted in Figures 7 and 8.

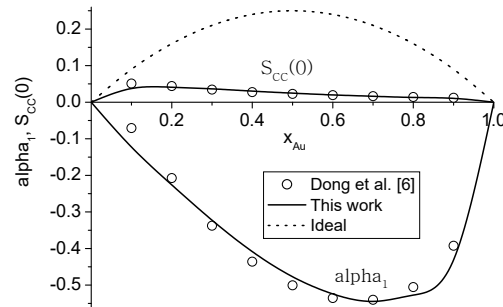


Figure 7: Computed values of  $S_{CC}(0)$  and  $\alpha_1$  of Au-La liquid alloy at 1473 K.

At a temperature and concentration, if  $S_{CC}(0) < S_{CC}^{id}(0)$ ,  $\alpha_1 < 0$  and  $D_M/D_{id} > 1$ , then complex formation tendency or hetero-coordinating tendency in the alloy is expected. At the same constraints, if  $S_{CC}(0) > S_{CC}^{id}(0)$ ,  $\alpha_1 > 0$  and  $D_M/D_{id} < 1$ , then self association among the atoms of alloy or homo-coordinating tendency is expected. The computed values of  $S_{CC}(0)$  showed negative deviation with respect to its ideal values in the entire concentration range indicating the system to be ordering in nature. This finding is further supported by the negative values of  $\alpha_1$  and  $D_M/D_{id} > 1$  (Figures 7 and 8). Moreover, the values of  $S_{CC}(0)$  and  $\alpha_1$  computed using the parameters of this work and Dong et al. [6] were found to be consistent with each other at all concentrations.

Following the similar procedure as mentioned above, the values of  $S_{CC}(0)$ ,  $\alpha_1$  and  $D_M/D_{id} > 1$  were computed in the temperature range 1473-1773 K. The compositional and temperature dependence of these functions are displayed in Figures 9-11.

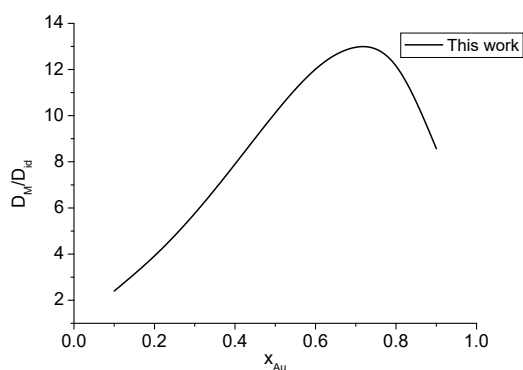


Figure 8: Computed values of  $D_M/D_{id}$  versus  $x_{Au}$  of Au-La liquid alloy at 1473 K.

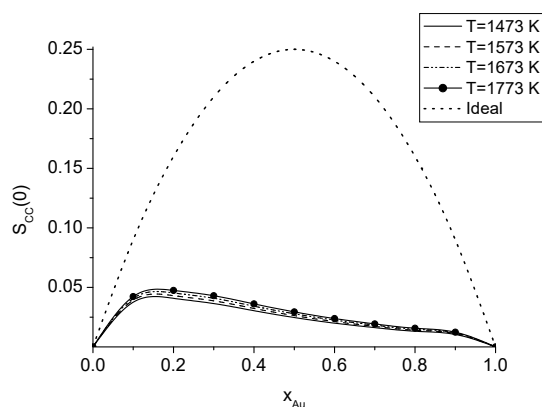


Figure 9:  $S_{CC}(0)$  versus  $x_{Au}$  of Au-La liquid alloy at different temperatures.

The computed values of  $S_{CC}(0)$  gradually increased and got closure to its ideal values with the rise in temperature of the system above its melting temperature (Figure 9). At equiatomic composition ( $x_{Au} = 0.5$ ), the deviation of  $S_{CC}(0)$  from  $S_{CC}^{id}(0)$  were found to be  $-0.22529$ ,  $-0.22370$ ,  $-0.22211$  and  $-0.22054$  at 1473 K, 1573 K, 1673 K and 1773 K respectively. These decrease in negative deviations correspond the decrease in in compound forming tendency in the initial melt at high temperatures.

This result is further supported by the decrease in negative values of  $\alpha_1$  and decrease in positive values of  $D_M/D_{id}$  with increase in temperature of the system (Figures 10 and 11). At  $x_{Au} = 0.5$ , the

computed values of  $\alpha_1$  were found to be  $-0.47692$ ,  $-0.45959$ ,  $-0.44331$  and  $-0.42814$  and those of  $D_M/D_{id}$  were computed to be 10.11753, 9.50450, 8.96344 and 8.48676 at 1473 K, 1573 K, 1673 K and 1773 K respectively. These results further stands in favour of those revealed by  $S_{CC}(0)$ . Thus, the results obtained from the investigations of structural functions are in accordance with those indicated by the thermodynamic functions in the above section.

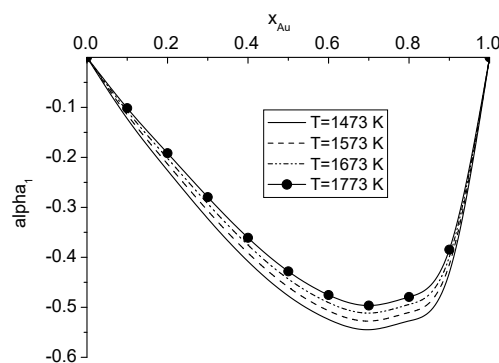


Figure 10:  $\alpha_1$  versus  $x_{Au}$  of Au-La liquid alloy at different temperatures.

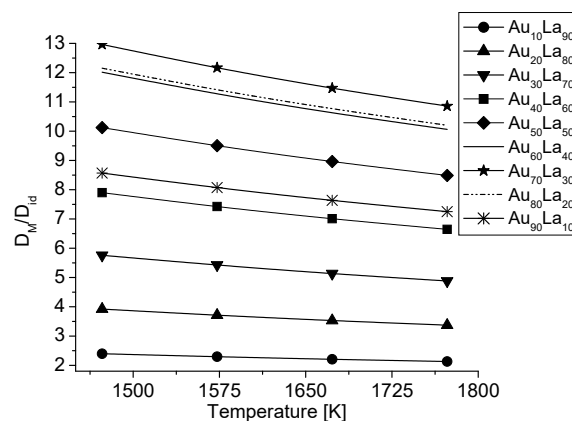


Figure 11: Computed values of  $D_M/D_{id}$  of Au-La liquid alloy at different temperatures.

### 3.3 Surface properties

In surface properties, surface tension ( $\sigma$ ) and extent of surface segregation (surface concentrations,  $x_i^s$ ) were computed in the frame work of Butler model [10, 24] using Equations (26-25) and parameters from Table 2. The compositional dependence of  $x_i^s$  and  $\sigma$  are portrayed in Figures 12 and 13 respectively.

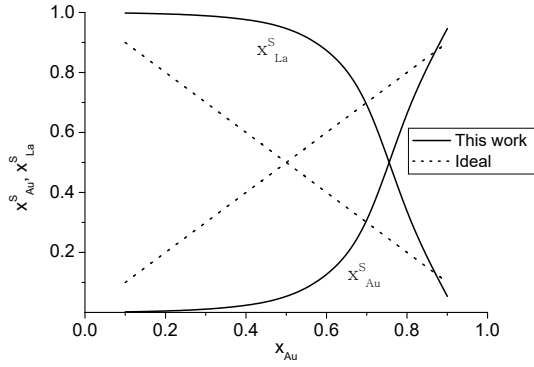


Figure 12: Computed values of  $x_{Au}^S$  and  $x_{La}^S$  versus  $x_{Au}$  of Au–La liquid alloy at 1473 K.

The surface concentration of La ( $x_{La}^S$ ) showed positive deviation whereas that of Au ( $x_{Au}^S$ ) showed negative deviation from their respective ideal values in the concentration range  $x_{Au}^S < 0.9$  (Figure 12). Among the two components, La has the lower surface tension ( $\sigma_{La} = 0.63360$  N/m) and that of Au is higher ( $\sigma_{Au} = 1.13475$  N/m) at 1473 K, melting temperature of the system. Therefore, La segregated in the surface phase and Au remained in the bulk phase of the initial melt in the range  $x_{Au}^S < 0.9$ .  $x_{Au}^S$  gradually increased and  $x_{La}^S$  gradually decreased with the increase in the bulk concentration of Au ( $x_{Au}$ ). They exceed their respective ideal values beyond  $x_{Au}^S > 0.9$  indicating exchange of their positions in the two phases of melt. The computed values  $\sigma$  of the system gradually increased with increased in the bulk concentration of Au. It showed negative deviation from its ideal value beyond  $x_{Au} < 0.6$  while showed positive deviation in the remaining range (Figure 13).

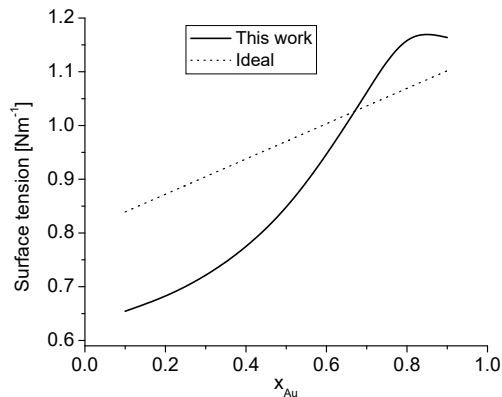


Figure 13: Compositional dependence of  $\sigma$  of Au–La liquid alloy at 1473 K.

Table 2: Input parameters for surface tension [25]

Atom	$T_0$ (K)	$\rho_0$ (kg/m <sup>3</sup> )	$\frac{\partial \rho}{\partial T}$ (kg/m <sup>3</sup> K)	$\sigma_0$ (N/m)	$\frac{\partial \sigma}{\partial T}$ (N/mK)
Au	1336	17360	-1.50	1.169	-0.00025
La	1203	5955	-0.24	0.720	-0.00032

The surface tension and surface concentrations of the components of the system were also calculated at different temperatures with the aid of Equations (26-25) and parameters from Table 2. The compositional and temperature dependence of estimated values are presented in Figures 14-16.

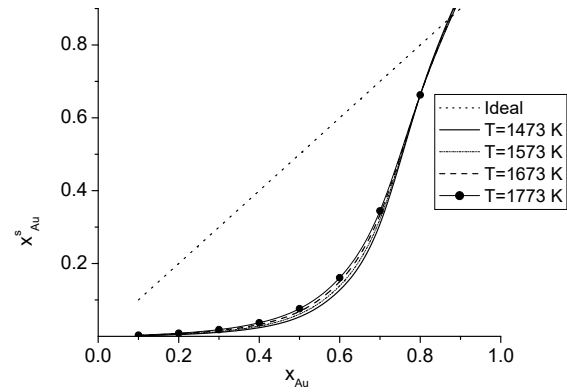


Figure 14: Computed values of  $x_{Au}^S$  versus  $x_{Au}$  of Au–La liquid alloy at different temperatures.

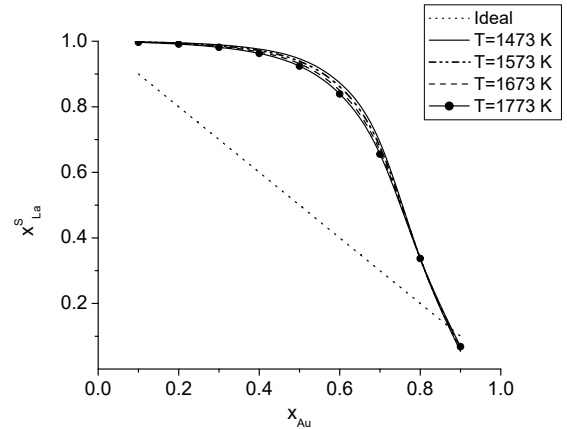


Figure 15: Computed values of  $x_{La}^S$  versus  $x_{Au}$  of Au–La liquid alloy at different temperatures.

The surface concentrations of Au gradually increased and those of La gradually decreased with increase in temperature of the liquid mixture. The negative deviations of  $x_{Au}$  and positive deviation of  $x_{La}$  from their respective ideal values eventually decreased at elevated temperature (Figure 14 and 15). Therefore, Au atoms move from bulk to surface phase while those of La moves from surface



to bulk phase to maintain the equilibrium condition in the liquid. Moreover, the surface tension of the mixture gradually decreased linearly with the increase in temperature beyond its melting temperature (Figure 16). These results are as expected since the cohesive force between the components of the liquid mixture gradually decreases with the increase in temperature.

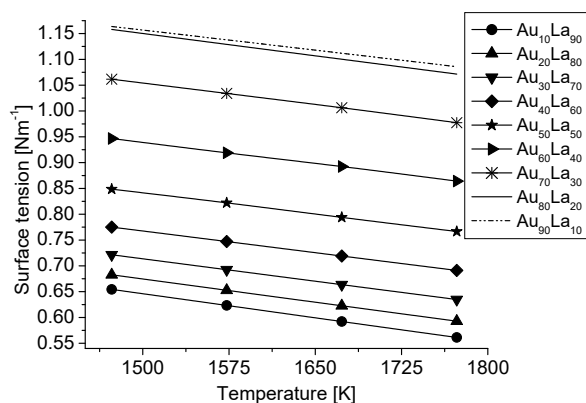


Figure 16: Variation of  $\sigma$  with temperature of Au-La liquid alloy.

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## 4 Conclusions

The preferred theoretical models, quasi-lattice and Butler's models, successfully explained the compositional and temperature dependence of thermodynamic, structural and surface properties of Au-La liquid alloy. The system was found to be the most interacting at its melting temperature whereas this tendency gradually decreased with increase in temperature. The surface tension of the system decreased linearly at elevated temperatures. The results obtained from the theoretical investigations of thermodynamic, structural and surface properties were in accordance with each other.

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