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# Thermodynamic, structural, surface and transport properties of Au-Ni liquid alloy at 1150 K

# S. K. Yadav, N. Chaudhary, D. Adhikari\*

Department of Physics, Mahendra Morang Adarsh Multiple Campus, Tribhuvan University, Biratnagar, Nepal.

\*Email: adksbdev@yahoo.com

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#### **ABSTRACT**

Thermodynamic, structural, surface and transport properties of Au-Ni liquid alloy at 1150 K were computed using different theoretical approaches. The thermodynamic properties, such as excess Gibbs free energy of mixing, enthalpy of mixing, activity and excess entropy of mixing and structural properties, such as concentration fluctuation in long wavelength limit and Warren-Cowley short range order parameter were computed in the frame work of Flory's model. The effect of positive and negative values of the interchange energy parameter on the excess Gibbs free energy of mixing and concentration fluctuation in long wave length limit was also observed. The surface tension and surface concentration of the system were calculated using Butler's model. In transport property, the viscosity of the system was calculated using Kaptay and Budai-Benko-Kaptay (BBK) models.

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# 1. Introduction

The comprehensive knowledge of the mixing behaviours of binary and multi-component liquid alloys are mandatory in order to develop new materials with desired characteristics. The study and explanation of the hetero-coordinating and homo-coordinating tendencies of the liquid alloys leading to different phase stabilities in the solid states are the most promising research directions in the metallurgical science and engineering. Several researchers [1-16] working in this field have long been attempting to reveal these behaviours by

developing different modelling equations or by correlating them. Therefore, an attempt has been made in this work to study and explain the mixing and demixing behaviours of Au-Ni liquid alloy at 1150 K using different theoretical approaches.

The thermodynamics of Au-Ni system have been studied by different authors [17–26]. But the complete set of mixing properties of the system is lacking till date. In this regard, the mixing behaviours of Au-Ni liquid alloy at 1150 K have been explained in terms of the thermodynamic, structural, surface and transport properties. The

thermodynamic and structural properties of the system were computed on the basis of Flory's model [11, 27]. The mixing and demixing behaviours of the binary liquid alloys are generally explained in terms of the thermodynamic and structural properties. The compound forming liquid alloys are characterised by high negative values of excess free energy of mixing  $(\Delta G_M^{xs})$  and enthalpy of mixing  $(\Delta H_M)$ . The activities (a) of such systems show negative deviation from the Raoult's law. Meanwhile, the liquid alloys showing demixing behaviours have positive or very low negative values of  $\Delta G_M^{xs}$  and  $\Delta H_M$ , and their activities show positive deviation from the Raoul'ts law [4, 28, 29]. Likewise, the study of structural properties has been developed as an important tool to explain and predict the nature of the local arrangements of liquid alloys. If the computed values of concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ) is less than the ideal value  $(S_{CC}^{id}(0))$ , i.e., if  $S_{CC}(0) < S_{CC}^{id}(0)$ , then heterocoordinating or ordering nature of the system is expected and if  $S_{CC}(0) > S_{CC}^{id}(0)$ , then homocoordinating or segregating nature of the system is expected. Consequently, the value of Warren-Cowley short range order parameter ( $\alpha_1$ ) is found to be non-zero and negative  $(\alpha_1 < 0)$  for ordering system,  $\alpha_1 > 0$  is found for segregating system and  $\alpha_1 = 0$  represents random mixing.

The surface properties and the viscosity of the liquid alloys are the direct consequences of their thermodynamic properties. Hence the surface properties, such as surface tension  $(\sigma)$  and the extent of surface segregation  $(x_i^s)$  of the system were computed using Butler's model [30-34]. The viscosity  $(\eta)$  of the system was computed on the basis of Kaptay [34, 35] and Budai-Benko-Kaptay (BBK) [36] models. The necessary theoretical formulations of the work are presented in the Section 2, the results and discussion are presented in the Section 3 and the conclusions are outlined in the Section 4.

# 2. Modeling Equations

# Thermodynamic properties

In thermodynamic properties, excess free energy of mixing ( $\Delta G_M^{xs}$ ), activities of monomers Al ( $a_{Al}$ ) and Ni ( $a_{Ni}$ ), enthalpy of mixing ( $\Delta H_M$ ) and excess entropy of mixing ( $\Delta S_M^{xs}$ ) have been analysed using Flory's model [11, 22]. This model is fundamentally used to explain the properties of alloys showing likeatoms clusters or self-associates. The preferred liquid alloy, Au-Ni at 1100 K also show the same behaviour. If  $\mu$  atoms of A (=Al) and v atoms of B (=Ni) are mixed near to their melting temperatures, then there are preferable associations among the like atoms in the metallic mixture of the types  $\mu A \leftrightharpoons A_{\mu}$  and  $v B \leftrightharpoons B_v$ , called self-associates. The expression for  $\Delta G_M^{xs}$  on the basis of the selected model can be given as

$$\Delta G_M^{xs} = RT \left[ \ln \frac{(1-\beta)^x}{(1-\beta x)} + \frac{x(1-x)}{(1-\beta x)} \omega \right]$$
 (1)

where R is the real gas constant, T is the absolute temperature, x is the composition of Al and  $\omega$  is the interchange energy. The term  $\beta$  is the size factor and is given as

$$\beta = \frac{(\phi - 1)}{\phi} \text{ with } \phi = \frac{\Omega_{\text{Ni}}}{\Omega_{\text{Au}}}$$
 (2)

where  $\Omega$  is the atomic size of the atom. The free energy of mixing  $(\Delta G_M)$  and excess free energy of the mixing  $(\Delta G_M^{xs})$  are related as

$$\Delta G_M = \Delta G_M^{xs} + RT[x \ln x + (1 - x) \ln(1 - x)]$$
(3)

The activity ( $a_i$ ; i = 1,2) of the i<sup>th</sup> component of the binary liquid alloy in terms of  $\Delta G_M$  is expressed as

$$RT \ln(a_i) = \Delta G_M + (1 - x) \left(\frac{\partial \Delta G_M}{\partial x}\right)$$
 (4)

Using Equations (1) and (3) in Equation (4), the expression for  $a_i$  can be obtained as

$$\ln a_i = \ln[(1 - \beta)(1 - x)\gamma(x)] + \beta(1 - x)\gamma(x) + \frac{\omega}{RT}(1 - x)^2[\gamma(x)]^2$$
 (5)

where  $\gamma(x) = 1/(1 - \beta x)$ .

The standard thermodynamic relation relating enthalpy of mixing, excess entropy of mixing and free energy of mixing are given as

$$\Delta H_M = \Delta G_M - T \left( \frac{\partial \Delta G_M}{\partial T} \right) \tag{6}$$

and 
$$\Delta S_M^{xs} = -\left(\frac{\partial \Delta G_M^{xs}}{\partial T}\right)$$
 (7)

Using Equations (1) and (3) in Equation (7), one can yield the respective expressions for  $\Delta H_M$  and  $\Delta S_M^{xs}$  as

$$\Delta H_{M} = \frac{x(1-x)\omega}{(1-\beta x)} - T \frac{x(1-x)}{(1-\beta x)} \frac{\partial \omega}{\partial T} + RT^{2} \frac{x(1-x)}{(1-\beta x)} \left[ \frac{\beta}{(1-\beta)} - \frac{x}{(1-\beta x)} \frac{\omega}{RT} \right] \frac{\partial \beta}{\partial T}$$

$$\Delta S_{M}^{xs} = \frac{RTx(1-x)}{(1-\beta x)} \left[ \frac{\beta}{(1-\beta)} - \frac{\omega x}{RT(1-\beta x)} \right] \frac{\partial \beta}{\partial T} - x(1-x) \frac{1}{(1-\beta x)} \frac{\partial \omega}{\partial T} - R[x \ln(1-\beta) - \ln(1-\beta x)]$$
(9)

where  $\frac{\partial \omega}{\partial T}$  and  $\frac{\partial \beta}{\partial T}$  are the temperature derivative terms of interchange energy and size factor respectively.

# Structural properties

To analyse the local arrangements of atoms in the metallic mixture, the concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ) and Warren-Cowley short range order parameter (WCSROP),  $\alpha_1$ , were calculated.  $S_{CC}(0)$  in terms of  $\Delta G_M$  can be expressed by standard thermodynamic relation as [37, 38]

$$S_{CC}(0) = RT \left(\frac{\partial^2 G_M}{\partial x^2}\right)^{-1} \tag{10}$$

Using Equations (1) and (3), the relation for  $S_{CC}(0)$  can be obtained as

$$S_{CC}(0) = \frac{x(1-x)}{1-x(1-x)f(\beta,\omega)}$$
(11)

where 
$$f(\beta, \omega) = \left[\frac{2\omega}{RT} \frac{(1-\beta)}{(1-\beta x)^3} - \frac{\beta^2}{(1-\beta x)^2}\right]$$
 (12)

Putting  $f(\beta, \omega) = 0$  in Equations (11) and (12), the expression for ideal value of  $S_{CC}(0)$  can be obtained as

$$S_{CC}^{id}(0) = x(1-x) \tag{13}$$

The experimental value of  $S_{CC}(0)$  can be calculated by the following relation

$$S_{CC}(0) = (1 - x) \frac{a_i}{\left(\frac{\partial a_i}{\partial x}\right)} = x \frac{a_j}{\left(\frac{\partial a_j}{\partial (1 - x)}\right)}$$
(14)

Herein,  $a_i$  and  $a_j$  are the experimental values of the activity of i<sup>th</sup>  $(a_{Au})$  and j<sup>th</sup>  $(a_{Ni})$  respectively.

The Warren-Cowley short range order parameter  $(\alpha_1)$  for binary liquid alloys can be given as [37, 38]

$$\alpha_1 = \frac{(S-1)}{[S(Z-1)+1]} \tag{15}$$

where *Z* is the coordination number and its value is taken to be 10 in present work and  $S = \frac{S_{CC}^{id}(0)}{S_{CC}(0)}$ .

# Surface properties

According to the Butler model, the surface tension  $(\sigma)$  of the binary liquid alloy in the initial melt can be expressed as [30-32]

$$\sigma = \sigma_1^0 + \frac{RT}{\varphi_1} \left[ \ln x_1^S - \ln x_1 \right] + \frac{\Delta G_{S,1}^{xs} - \Delta G_1^{xs}}{\varphi_1}$$
 (16)

$$\sigma = \sigma_2^0 + \frac{RT}{\varphi_2} \left[ \ln x_2^S - \ln x_2 \right] + \frac{\Delta G_{s,2}^{xs} - \Delta G_2^{xs}}{\varphi_2}$$
 (17)

where  $\sigma_i^0$  (i=1,2) is the surface tension of the pure atom i,  $\varphi_i$  is the molar surface area of pure atom i and  $x_i^S$  and  $x_i$  are the surface and bulk concentrations of atoms i in the surface phase and bulk phase of the liquid alloy respectively.  $\Delta G_{s,i}^{xs}$  is the surface partial excess free energy of atom i and  $\Delta G_i^{xs}$  is the bulk partial excess free energy of atom i and they are related as  $\Delta G_{s,i}^{xs} = \beta \Delta G_i^{xs}$ , where  $\beta$  is constant and  $\beta = 0.83$  [28, 32, 34, 39] is taken for calculations in the present work.

The molar surface area of ith atom is expressed as

$$\varphi_i = 1.091 \left( V_i^0 \right)^{2/3} (N_A)^{1/3} \tag{18}$$

where  $V_i^0$  is the molar volume of i<sup>th</sup> atom and  $N_A = N$  is the Avogadro's number. The molar volume  $(V_i^0)$  of i<sup>th</sup> atom is calculated by taking the ratio of its mass  $(m_i)$  and density  $(\rho_i^0)$  at the required temperature  $(T_K)$ . The temperature dependent expressions of  $\sigma_i^0$  and  $\rho_i^0$  can be given as [40]

$$\sigma_i^0 = \sigma_0 + (T_K - T_0) \frac{d\sigma}{dT}$$
  
and  $\rho_i^0 = \rho_0 + (T_K - T_0) \frac{d\rho}{dT}$  (19)

Herein,  $\sigma_0$  and  $\rho_0$  are the surface tension and density of the pure atom at its melting temperature,  $T_0$  is the melting temperature of the pure atom and  $\frac{d\sigma}{dT}$  and  $\frac{d\rho}{dT}$  are the temperature derivative terms of surface tension and density respectively.

#### **Transport property**

In transport property, the viscosity  $(\eta)$  of the system was calculated using Kaptay equation [34,35] and

Budai-Benko-Kaptay (BBK) model [36]. According to the Kaptay model, the expression for the viscosity of the binary liquid alloys can be given by

$$\eta = \left(\frac{h N_A}{\sum_i x_i V_i^0 + V^E}\right) \exp\left(\frac{\sum_i x_i G_i^* - (0.155 \pm 0.015) H_M}{RT}\right)$$
(20)

where h is Planck's constant and  $V^E$  is the excess volume of alloy formation which can be neglected. The term  $G_i^*$  stands for the Gibb's energy of activation of the viscous flow of  $i^{th}$  component and is expressed as

$$G_i^* = RT \ln \left( \frac{\eta_i^0 V_i^0}{hN_A} \right) \tag{21}$$

where  $\eta_i^0$  is the viscosity of the pure component of the metallic mixture and can be given as [40]

$$\eta_i^0 = \eta_0 \exp(\frac{E}{PT}) \tag{22}$$

where  $\eta_0$  is the viscosity of the pure atom at its melting temperature and E is the activation energy. The ideal value of the viscosity of the liquid mixture can be expressed as

$$\eta^{id} = \sum_{i} x_i \, \eta_i^0 \tag{23}$$

Following Budai-Benko-Kaptay [36], the expression for the viscosity of binary liquid alloy can be given as

$$\eta = A. \frac{(\sum_{i} x_{i} M_{i})^{1/2}}{(\sum_{i} x_{i} V_{i} + V^{E})^{2/3}} T^{1/2} \exp\left[\frac{B}{T} \left(\sum_{i} x_{i} T_{m,i}^{*} - \frac{\Delta H_{M}}{q.R}\right)\right]$$
(24)

where q=25.4 is the semi-empirical parameter which is related to the cohesion energy of the pure liquid metal and  $T_{m,i}^*$  is defined as effective melting point of the pure component. The values of the coefficients A and B can be taken as  $(1.8 \pm 0.39) \times 10^8$  and  $(2.34 \pm 0.2)$  respectively

#### 3. Results and Discussion

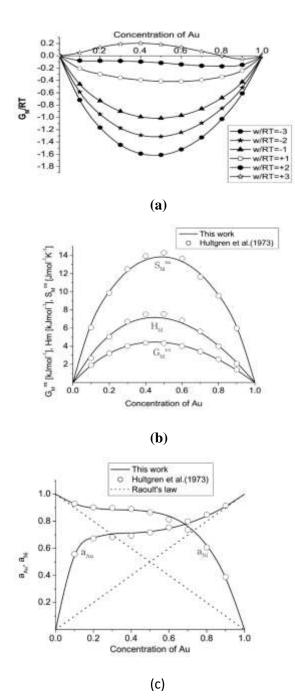
The value of  $\phi = 1.63$  was first calculated using Equation (2) and then the effect of interchange energy ( $\omega$ ) on free energy of mixing ( $\Delta G_M$ ) was observed. For this purpose, the values of  $\Delta G_M$  were computed using Equations (1-3) for different values of  $\omega$ , such as  $\pm 3RT$ ,  $\pm 2RT$  and  $\pm 1RT$ . The plot of the isotherms of the compositional dependence of  $\Delta G_M$  for aforementioned values of  $\omega$  at 1150 K is

portrayed in Fig. 1(a). It can be observed that the negative values  $\Delta G_M$  gradually increases with the increase in the negative values of  $\omega$  and decreases with increase in the positive values of  $\omega$ . The value of  $\Delta G_M$  is found to be positive for  $x_{Au} = x < 0.8$  for  $\omega = +3RT$ .

The optimised value of  $\omega = 15400$  and  $\beta = 0.32886$  were then obtained using Equations (1-3) and the experimental value of  $\Delta G_M^{xs}$  [29] employing the method of successive approximation. The experimental and the calculated values of  $\Delta G_M^{xs}$  were found to be in well agreement (Fig. 1(b)). Both of these values are found to be positive which correspond that the Au-Ni liquid alloy at 1150 K is a homo-coordinating or segregating system. Hence, the system shows demixing tendency with respect to the thermodynamic functions. The like-atoms clusters or self-associates are favourable in the liquid state and the system exhibit liquid miscibility gaps [4].

The activity of the system was computed using Equations (5) and above determined model parameters. The experimental [29] as well as the theoretical values of activities of the monomers Au  $(a_{Au})$  and Ni  $(a_{Ni})$  were found to be in well agreement (Fig. 1(c)). Both of these values show positive deviation from Raoult's law indicating that the preferred system is segregating in nature. Theoretical investigations show that the model parameters have successfully reproduced excess free energy of mixing and activity of the system.

The temperature derivative terms of model parameters  $(\frac{\partial \omega}{\partial T} = -7.2000 \text{ and } \frac{\partial \beta}{\partial T} = -0.00001)$  were optimised using Equation (8) and the experimental value of the enthalpy of mixing  $(\Delta H_M)$  [29]. The enthalpy of mixing  $(\Delta H_M)$  and the excess entropy of mixing  $(\Delta S_M^{xs})$  were then computed using Equations (8) and (9) respectively with the aid of abovementioned model parameters. Both of these values are found to be in good agreement with their respective experimental values (Fig. 1 (b)). Moreover, the positive value of  $\Delta H_M$  reveals the demixing tendency of the system.



**Fig. 1(a-c):** Plots of the compositional dependence of thermodynamic functions for Au-Ni liquid alloys at 1150 K. (a) Effect of positive and negative values of  $\omega/RT$  on  $\Delta G_M$ , (b)  $\Delta G_M^{xs}$ ,  $\Delta H_M$  and  $\Delta S_M$  and (c)  $a_{Au}$  and  $a_{Ni}$ .

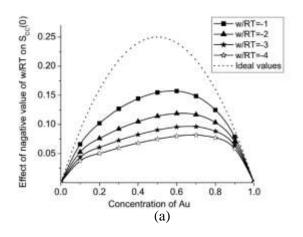
The greater insight of the homo-coordinating and hetero-coordinating nature of the liquid alloys can be obtained by computing and analysing the structural functions. For this purpose, the theoretical, ideal and experimental values of the concentration fluctuation in long wavelength limit ( $S_{CC}(0)$ ) were computed using Equations (11-14) with the help of abovementioned model parameters and the experimental value of activity [29].

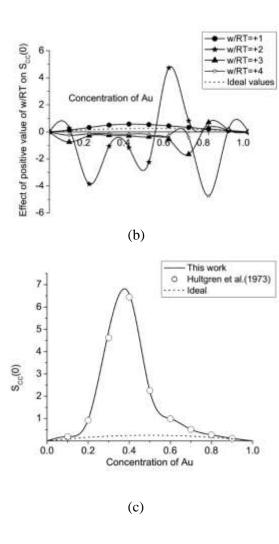
The effect of the positive and the negative values of  $\omega$  on  $S_{CC}(0)$  were studied by arbitrarily varying the values of as  $\omega = \pm 4RT, \pm 3RT, \pm 2RT$  and  $\pm 1RT$ . It can be observed that with gradual increase in the negative values of  $\omega$ , the deviation between the ideal and the theoretical values of  $S_{CC}(0)$  gradually increases (Fig. 2(a)). These results predict that the preferred system would turn into segregating to ordering nature with increase in the negative value of  $\omega$ . Likewise, the effect of positive values of  $\omega$  on  $S_{CC}(0)$  as a function of concentration is presented in Fig. 2(b). It indicates that the computed values of  $S_{CC}(0)$  gradually increases and reaches the peak value at x = 0.4 for  $\omega = +1RT$ . For  $\omega = +2RT$ ,  $S_{CC}(0)$  is found to have negative value in the range 0.1 < x < 0.53. Likewise, for  $\omega = +3RT$ ,  $S_{CC}(0)$ is found to be negative in the range x < 0.9 and for  $\omega = +4RT$ , it is found to be negative in the range 0.1 < x < 0.62, 0.69 < x < 0.9. As  $S_{CC}(0)$  cannot have negative values, the value of interchange energy should be in between 1 and 2, i.e., +1RT < $\omega < +2RT$ . The same result ( $\omega = +1.6107RT$ ) was found during the investigation of the thermodynamic properties.

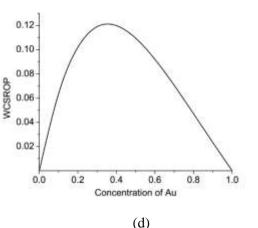
The theoretical as well experimental computed values of  $S_{CC}(0)$  are in excellent agreement and are found to be grater than the ideal value at all concentrations (Fig. 2(c)). Therefore, it can be concluded that the liquid Au-Ni at 1150 K shows complete homo-coordinating tendency. The theoretical values of WCSROP ( $\alpha_1$ ) were computed using Equation (15) and plotted in Fig. 2(d). The value of  $\alpha_1 > 1$  at all compositions revealing the similar nature as by  $S_{CC}(0)$ . Thus, the theoretical findings of thermodynamic and structural properties are in accordance and suggest the demixing behaviour of the system at selected temperature.

surface tension  $(\sigma)$  and concentrations of the monomers Au  $(x_{Au}^s)$  and Ni  $(x_{Ni}^s)$  were computed using Butler's model [30]. The surface tensions and densities of the pure components of the system were computed using Equation (19) and the parameters in Table 1. The values of  $\sigma$ ,  $x_{Au}^{s}$  and  $x_{Ni}^{s}$  were then computed using Equations (17) and (18). The ideal value of the surface tension ( $\sigma^{id}$ ) of the liquid alloy is obtained as the additive sum of the surface tension of the pure atoms in it using the relation  $\sigma^{id} = \sum_i x_i \, \sigma_i^0$ . The surface concentration of Au atom is found to be higher whereas that of Ni is found to be lower than their respective ideal values (Fig. 3(a)). Therefore, Au atoms segregates on the surface phase and Ni atoms remains in the bulk phase in the initial melt. The computed values of the surface tension of the system is found to be less than the ideal value at all compositions (Fig. 3(b)).

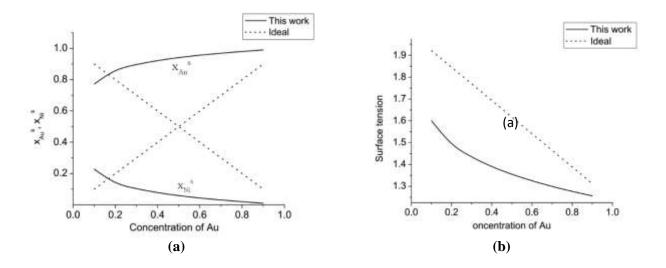
In transport property, the viscosity  $(\eta)$  of the system was computed using Kaptay model [34,35] and Budai-Benko-Kaptay (BBK) model [36]. The viscosity is directly related to the enthalpy of mixing of the system and is the measure of the cohesion energy of the metallic solution. The viscosity  $(\eta)$  and its necessary ingredients for the system was computed using Equations (20-24) with the help of the input parameters from Table 1. The computed values of the viscosity of the system from both of the preferred models are found to be less than the ideal value at all compositions (Fig. 4).



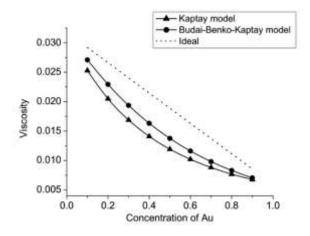




**Fig. 2(a-d):** Plots of the compositional dependence of structural functions for Au-Ni liquid alloy at 1150 K. (a) Effect of negative values of  $\omega/RT$  on  $S_{CC}(0)$ , (b) Effect of positive values of  $\omega/RT$  on  $S_{CC}(0)$ , (c)  $S_{CC}(0)$  and (d) WCSROP.



**3(a, b):** Plots of the compositional dependence of the surface tension ( $\sigma$ ) and surface concentrations ( $x_{Au}^s$  and  $x_{Ni}^s$ ) for Au-Ni liquid alloy at 1150 K. (a) Surface tension and (b) Surface concentrations



**Fig. 4:** The compositional dependence of viscosity  $(\eta)$  for Au-Ni liquid alloy at 1150 K.

**Table 1:** Input parameters for surface tension ( $\sigma$ ) and viscosity ( $\eta$ ) [40]

Metal	$T_0$	$ ho_0$	$\partial \rho / \partial T$	$\sigma_0$	$\partial \sigma/\partial T$	$\eta_0$	E
	(K)	$(kg m^{-3})$	$(kg m^{-3} K^{-1})$	$(N m^{-1})$	$(N m^{-1} K^{-1})$	$(Nsm^{-2})$	$(Jmol^{-1})$
Au	1336	17360	-1.50	0.1140	-0.00052	0.001132	15900
Ni	1727	7905	-1.160	0.1778	-0.00038	0.0001663	50200

#### 4. Conclusion

The computed values of the excess free energy of mixing and the enthalpy of mixing were found to be positive and the activity showed positive deviation from the Raoult's law. The value of the concentration fluctuations in long wavelength limit was found to be greater than the ideal value and Warren-Cowley short range order parameter was found to be positive. These results correspond that the liquid Au-Ni alloy at 1150 K showed homocoordinating behaviours. The computed value of surface tension and viscosity were less than the ideal values. In the initial melt, Au atoms segregates in the surface phase whereas Ni atoms remains in the bulk phase.

#### References

- [1] A.B. Bhatia, R.N. Singh, A Quasi-lattice Theory for Compound Forming Molten Alloys, Phys. Chem. Liq. 13 (1984) 177. https://doi.org/10.1080/00319108408080778
- [2] W. Young, *Liquid metalls*. London: Institute of Physics, 1976.
- [3] R.N. Singh, I.S. Jha, S. Sinha, The segregation—ordering transformation in CdNa liquid alloys, J. Phys. Condens. Mat. 3 (1991). https://doi.org/10.1088/0953-8984/3/16/017
- [4] R.N. Singh, F. Sommer, Segregation and immiscibility in liquid binary alloys, Rep. Prog. Phys. 60 (1997) 57. https://doi.org/10.1088/0034-4885/60/1/003
- [5] D. Adhikari, Disorder in liquid Cu-Pd alloys, Phase Transitions 84 (2011) 308. https://doi.org/10.1080/01411594.2010.536088
- [6] E. Moelwyn-Hughes, Physical Chemistry. Oxford: Pergamon Press, 1961.
- [7] M.L. Huggins, Thermodynamic properties of solutions of long-chain compounds, Ann. New York Acad. Sci. 43 (1942) 1. https://doi.org/10.1111/j.1749-6632.1942.tb47940.x
- [8] A.S. Jordan, A theory of regular associated solutions applied to the liquidus curves of the Zn-Te and Cd-Te systems, Metall. Trans. 1 (1970) 239.
  - https://doi.org/10.1007/BF02819267

- [9] A.B. Bhatia, W.H. Hargrove, Concentration fluctuations and thermodynamic properties of some compound forming binary molten systems, Phys. Rev. B 10 (1974) 3186. https://doi.org/10.1103/PhysRevB.10.3186
- [10] R.P. Godbole, S.A. Jha, M. Milanarun, A.K. Mishra, Thermodynamics of liquid Cu Mg alloys, J. Alloys Compd. 363 (2004) 182. https://doi.org/10.1016/S0925-8388(03)00326-8
- [11] P.J. Flory, Thermodynamics of high polymers solutions, J. Chem. Phys. 10 (1942) 51.
- [12] A.B. Bhatia, W.H. Hargrove, D.E. Thornton, Concentration fluctuations and partial structure factors of compound-forming binary molten alloys, Phys. Rev. B 9 (1974) 435. https://doi.org/10.1103/PhysRevB.9.435
- [13] J. Alonso, N.H. March, Concentration fluctuations in simple metallic liquid alloys, Phys. B+C, 114 (1982) 67.

# https://doi.org/10.1016/0378-4363(82)90008-0

- [14] S.K. Yadav, L.N. Jha, D. Adhikari, Thermodynamic and Structural Behaviour of Mg-Ga Melt at 923 K, J. Adv. Phys. 3 (2014) 248.
  - https://doi.org/10.1166/jap.2014.1133
- [15] D. Adhikari, S.K. Yadav, L.N. Jha, Thermophysical properties of Al-Fe melt, J. Chinese Adv. Mater. Soc. 2 (2014) 149.
  - https://doi.org/10.1080/22243682.2014.928603
- [16] S.K. Yadav, L.N. Jha, D. Adhikari, Segregating to ordering transformation in In – Sn melt, Phys. Chem. Liq. 53 (2015) 37. https://doi.org/10.1080/00319104.2014.999337
- [17] M. Bienzle, T. Oishi, F. Sommer, Thermodynamics and local atomic arrangements of gold-nickel alloys, J. Alloys Compd. 220 (1995) 182.
  - https://doi.org/10.1016/0925-8388(94)06003-7
- [18] J. Wang, L.B. Liu, H.S. Liu, Z.P. Jin, Assessment of the diffusional mobilities in the face-centred cubic Au-Ni alloys, Calphad Comput. Coupling Phase Diagrams Thermochem. 31 (2007) 249. https://doi.org/10.1016/j.calphad.2006.11.006
- [19] J.L. Fattebert, M.E. Wickett, P.E.A. Turchi, Phase-field modeling of coring during solidification of Au-Ni alloy using quaternions and CALPHAD input, Acta Mater. 62 (2014) 89. <a href="https://doi.org/10.1016/j.actamat.2013.09.036">https://doi.org/10.1016/j.actamat.2013.09.036</a>
- [20] J. Davoodi, F. Katouzi, High pressure molecular

dynamics simulation of Au-x%Ni alloys, J. Appl. Phys. 115 (2014) 094905.

# https://doi.org/10.1063/1.4866596

- [21] J. Sopoušek et al., Au-Ni nanoparticles: Phase diagram prediction, synthesis, characterization, and thermal stability, Calphad: Comput. Coupling Phase Diagrams Thermochem. 58 (2017) 25.
  - https://doi.org/10.1016/j.calphad.2017.05.002
- [22] R. Willnecker, G.P. Görler, G. Wilde, [33] Appearance of a hypercooled liquid region for completely miscible alloys, Mater. Sci. Eng. A 226 (1997) 439.

# https://doi.org/10.1016/s0921-5093(97)80054-8

- [23] J. Wang, X.G. Lu, B. Sundman, X. Su, Thermodynamic assessment of the Au-Ni system, Calphad: Comput. Coupling Phase Diagrams Thermochem. 29 (2005) 263.
  - https://doi.org/10.1016/j.calphad.2005.09.004
- [24] W. Desorbo, Calorimetric investigations of a gold-nickel alloy. I. Low temperature heat capacity of gold-nickel alloy, Acta Metall. 3 (1955) 227.
  - https://doi.org/10.1016/0001-6160(55)90056-0
- [25] L. Topor, O. J. Kleppa, Thermochemistry of binary liquid gold alloys: The systems Au-Ni, Au-Co, Au-Fe, and Au-Mn, Metall. Trans. B 15 (1984) 573.

#### https://doi.org/10.1007/BF02657389

- [26] G.F. Day, R. Hultgren, Thermodynamics of the gold-nickel system, J. Phys. Chem. 66 (1962) 1532.
  - https://doi.org/10.1021/j100814a036
- [27] A.B. Bhatia, N.H. March, Size effects, peaks in concentration fluctuations and liquidus curves of Na–Cs, J. Phys. F Met. Phys. 5 (1975)1100.
- [28] U. Mehta, S.K. Yadav, I. Koirala, D. Adhikari, Thermo-physical properties of ternary Al – Cu – Fe alloy in liquid state, Philos. Mag. (2020). <a href="https://doi.org/10.1080/14786435.2020.1775907">https://doi.org/10.1080/14786435.2020.1775907</a>
- [29] R. Hultgren, P.D. Desai, D.T. Hawkins, M. Gleiser, K.K. Kelley, Selected Values of the Thermodynamic Properties of Binary Alloys. Ohio: ASM, Metal Park, 1973.
- [30] J.A.V. Butler, The thermodynamics of the surfaces of solutions, Proc. R. Soc. London A, 135 (1932) 348.
- [31] S.K. Yadav, L.N. Jha, D. Adhikari, Theoretical Modeling to Predict the Thermodynamic ,

Structural , Surface and Transport Properties of the Liquid Tl – Na Alloys at different Temperatures, J. Nepal Physical Soc. 4 (2017)

#### https://doi.org/10.3126/jnphyssoc.v4i1.17344

[32] G. Kaptay, Improved derivation of the Butler equations for surface tension of solutions, Langmuir, 35 (2019) 10987.

#### https://doi.org/10.1021/acs.langmuir.9b01892

33] R. Novakovic, Thermodynamic, surface properties and microscopic functions of liquid Al–Nb and Nb–Ti alloys, J. Non–Crystalline Solids 356 (2010)1593.

#### https://doi.org/10.1016/j.jnoncrysol.2010.05.055

[34] S.K. Yadav, L.N. Jha, D. Adhikari, Thermodynamic, structural, transport and surface properties of Pb- Tl liquid alloy, BIBECHANA 13 (2016)100.

# https://doi.org/10.3126/bibechana.v13i0.13443

- [35] G. Kaptay, Proceeding of micro CAD 2003 conference, International Conference, Section, Metallurgy (2003) 23.
- [36] I. Budai, M.Z. Benko, G. Kaptay, Comparison of different theoretical models to experimental data on viscosity of binary liquid alloys, Mater. Sci. Forum 537 (2007) 489.
  - https://doi.org/10.4028/www.scientific.net/MSF. 537-538.489
- [37] S.K. Yadav, L.N. Jha, D. Adhikari, Thermodynamic and structural properties of Bibased liquid alloys, Physica B: Phys. Condens. Mat. 475 (2015) 40. https://doi.org/10.1016/j.physb.2015.06.015
- [38] S.K. Yadav, S. Lamichhane, L.N. Jha, N.P. Adhikari, D. Adhikari, Mixing behaviour of Ni Al melt at 1873 K, Phys. Chem. Liq., 54 (2016) 370.

#### https://doi.org/10.1080/00319104.2015.1095640

[39] S.K. Yadav, L.N. Jha, I.S. Jha, B.P. Singh, R.P. Koirala, D. Adhikari, Prediction of thermodynamic and surface properties of Pb–Hg liquid alloys at different temperatures, Philos. Mag. 96 (2016) 1909.

#### https://doi.org/10.1080/14786435.2016.1181281

E. A. Brandes and G. B. Brook, *Smithells Metals Reference Book*, 7th ed. Jordan Hill, Oxford: Butterworth-Heinemann, 1992.

[40]